- 1. Given are the following data:
  - $C_{f} \coloneqq 98 \qquad \qquad C_{f} = Fixed cost$   $C_{v}(x) \coloneqq x^{3} 12x^{2} + 60x \qquad \qquad C_{v} = Variable cost$   $C(x) \coloneqq C_{f} + C_{v}(x) \qquad \qquad C = Cost$

Determine for x := 0..10[x = quantity] the values C(x) and C(x+1) - C(x).

- 2. Determine for x := 1..10 and for the function  $C(x) := 98 + 60x 12x^2 + x^3$  the values:
  - $c_v(x) := \frac{C_v(x)}{x} \qquad \quad c_v = \text{variable cost per unit}$

$$c_f(x) := \frac{C_f}{x} \qquad \qquad c_f = \text{fixed cost per unit}$$

$$c(x) := \frac{C(x)}{x}$$
 c = total cost per unit

Determine the quantity at which  $\boldsymbol{c}_v$  is a minimum and at which  $\boldsymbol{c}$  is a minimum.

3. Given are the following data

$$C_f := 50000$$

$$C_{v}(x) := 7000x - 180x^{2} + 2x^{3}$$

$$\mathbf{C}(\mathbf{x}) \coloneqq \mathbf{C}_{\mathbf{f}} + \mathbf{C}_{\mathbf{V}}(\mathbf{x})$$

At which quantity is the minimum of of the first derivative of C(x), the minimum of  $c_v(x)$  and the minimum of c(x)?

## Assignment to 2.5





How can the minima of C',  $c_{\rm v}$  and c be found graphically? You may make use of the following figures.







5. Given are the following data:

$$C_{f} := 2000$$

$$C_v(x) \coloneqq 0.2x^2$$

$$\mathbf{C}(\mathbf{x}) \coloneqq \mathbf{C}_{\mathbf{f}} + \mathbf{C}_{\mathbf{v}}(\mathbf{x})$$

Which is the the value of  $c_v$  for  $x_0 := 80$ ?

If  $c_v(x_0)$  were regarded as a constant, what would the cost function look like? Use the following figure to draw this cost function.



6. Given are the following data:

$$C_{f} := 2000$$

$$C_v(x) := 0.2x^2$$

$$\mathbf{C}(\mathbf{x}) \coloneqq \mathbf{C}_{\mathbf{f}} + \mathbf{C}_{\mathbf{V}}(\mathbf{x})$$

Which is the value of C' for  $\,x_0^{}=\,80\,$  ?

If  $C'(x_0)$  were regarded as a constant, what would the cost function look like? Use the following figure to draw this cost function.

Assignment to 2.5

