Assignment to 6.2.4.2 - Solution -

Given are the following data of a product:

 $c_v := 8$ Variable cost per unit

 $C_f := 6000$ Fixed cost

 $x_0 := 100$ Quantity of goods produced and of goods sold

The profit is:

$$R(x_0) := p \cdot x_0 - c_v \cdot x_0 - C_f$$

 $R(x_0) = 200$

For the quantity $x_1 := 97$ the profit is

$$R(x_1) := p \cdot x_1 - c_V \cdot x_1 - C_f$$

$$R(x_1) = 14$$

The difference in profit ist

$$\Delta \mathbf{R} := \mathbf{R}(\mathbf{x}_1) - \mathbf{R}(\mathbf{x}_0)$$

 $\Delta R = -186$

Generally the difference is

$$\Delta \mathbf{R} \coloneqq (\mathbf{p} - \mathbf{c}_{\mathbf{v}}) \cdot \mathbf{x}_{1} - \mathbf{C}_{\mathbf{f}} - (\mathbf{p} - \mathbf{c}_{\mathbf{v}}) \cdot \mathbf{x}_{0} + \mathbf{C}_{\mathbf{f}}$$
$$\Delta \mathbf{R} \coloneqq (\mathbf{p} - \mathbf{c}_{\mathbf{v}}) \cdot \mathbf{x}_{1} - (\mathbf{p} - \mathbf{c}_{\mathbf{v}}) \cdot \mathbf{x}_{0}$$
$$\Delta \mathbf{R} \coloneqq (\mathbf{p} - \mathbf{c}_{\mathbf{v}}) \cdot (\mathbf{x}_{1} - \mathbf{x}_{0})$$

If the difference in quantity is denominated by

$$\Delta \mathbf{x} := \mathbf{x}_1 - \mathbf{x}_0$$

$$\Delta x = -3$$

the differenc in result is

$$\Delta \mathbf{R} := \left(\mathbf{p} - \mathbf{c}_{\mathbf{V}}\right) \cdot \Delta \mathbf{x}$$

$$\Delta R = -186$$