

Law of Large Numbers

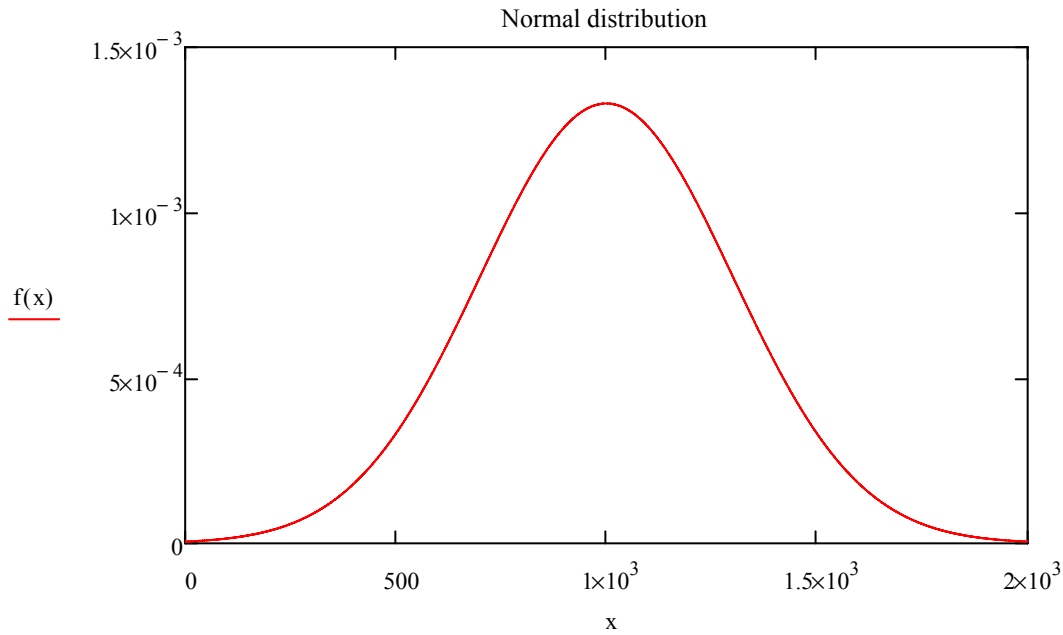
$x := 0..2000$ Random variable

$\mu := 1000$ Expected value of the random variable

$\sigma := 300$ Standard deviation of the random variable

$$f(x) := \frac{1}{\sigma \cdot \sqrt{2 \cdot \pi}} \cdot e^{-0.5 \cdot \left(\frac{x-\mu}{\sigma}\right)^2}$$

Probability distribution of the random variable (normal distribution)



$n := 10$ Number of values drawn from the probability distribution

$x := \text{rnorm}(n, \mu, \sigma)$ Random generator

Actual values of random variable

	1
1	868
2	796
3	858
4	715
5	494
6	1013
7	964
8	1167
9	1658
10	1243

$$x_d := \frac{1}{n} \cdot \sum x$$

Average actual value

$$x_d = 978$$

According to the central limit theorem (law of large numbers) the average actual value approaches the expected value, when the number of values drawn from the probability distribution approaches infinity:

$$\lim_{n \rightarrow \infty} x_d = \mu$$